

Magneto-thermal modeling of multilayer HTS tapes for their control at room temperature

Walid Dirahoui, Hocine Menana, Melika Hinaje

Université de Lorraine, GREEN, F-54000 Nancy, France

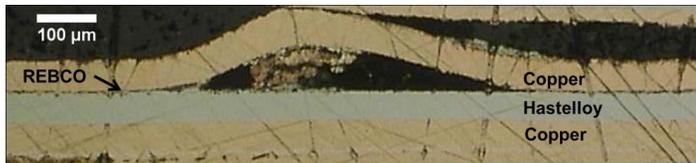
Outlines

- Introduction
- Experimental setup
- Modeling
- Results and validation
- Conclusion

Introduction

Context

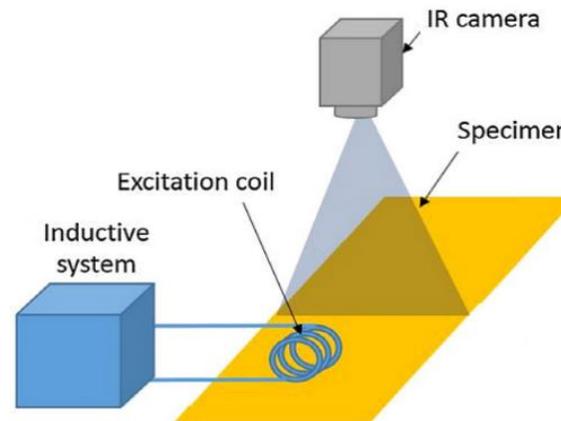
- Structural defects may lead to a substantial degradation of the performances of the HTS tapes.



Photograph of a cross-section of a delaminated sample

Objective

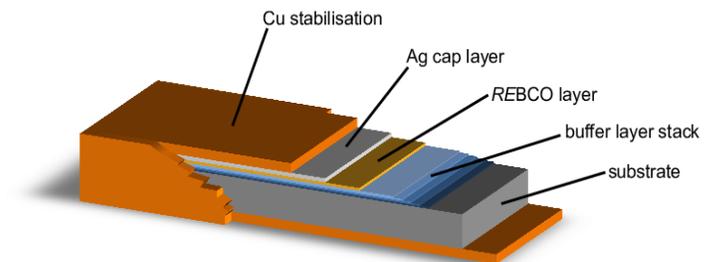
- NDT control of 2G HTS tapes by using eddy current thermography (ECT) at room temperature.



Schematic diagram of an ECT control device

Scientific and technical issues

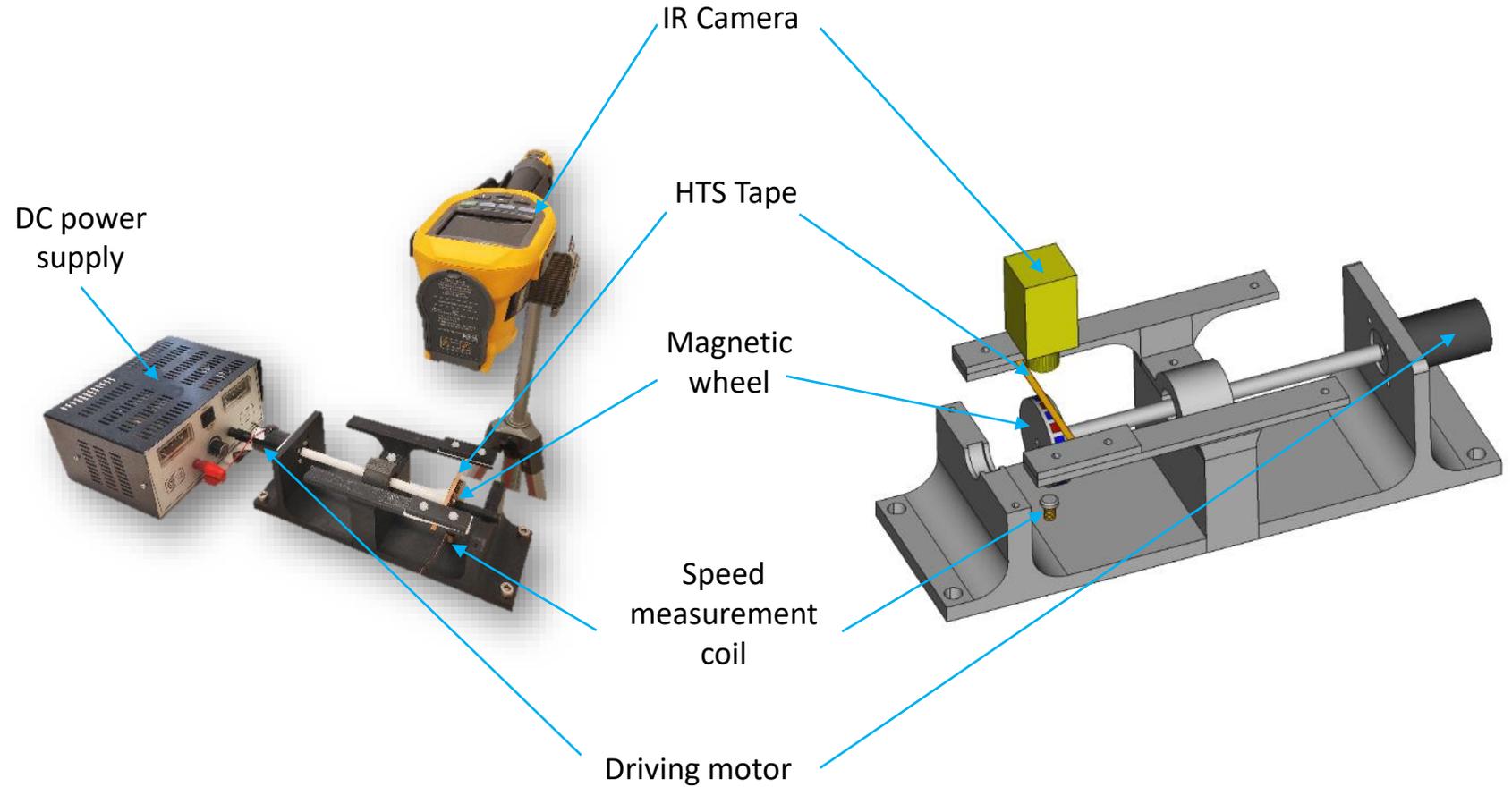
- Thin multilayered structure.
- Multiscale dimensions.
- Materials with different physical properties.



Typical structure of REBCO HTS tape

Experimental setup

- Avoid the thermal disturbances of current supplied inductors.
- Rotating magnetic wheel.



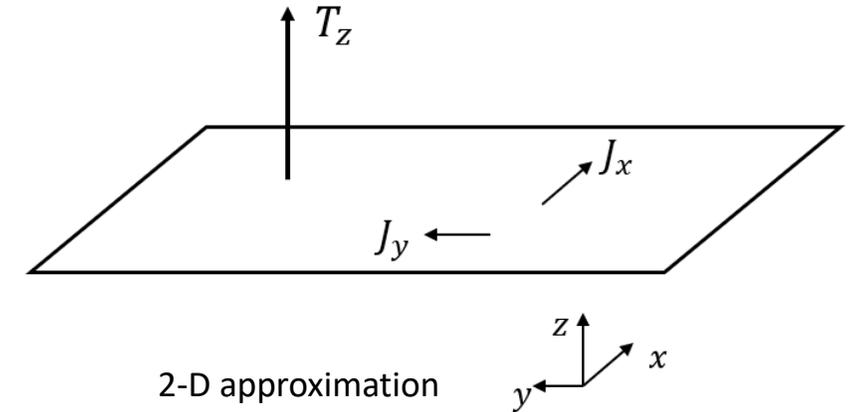
Photograph and schematic draw of the experimental setup

Modeling

Electromagnetic model

- Eddy currents:

$$\vec{\nabla} \times \vec{\sigma}^{-1} \vec{\nabla} \times \vec{T}_z = -\partial_t \left(\vec{B}_z^s + \frac{\mu_0}{4\pi} \int_v \frac{\vec{\nabla} \times \vec{T}_z \times \vec{r}}{r^3} dv \right) \quad \longrightarrow \quad \begin{cases} J_x = \frac{\partial T_z}{\partial y} \\ J_y = -\frac{\partial T_z}{\partial x} \end{cases}$$

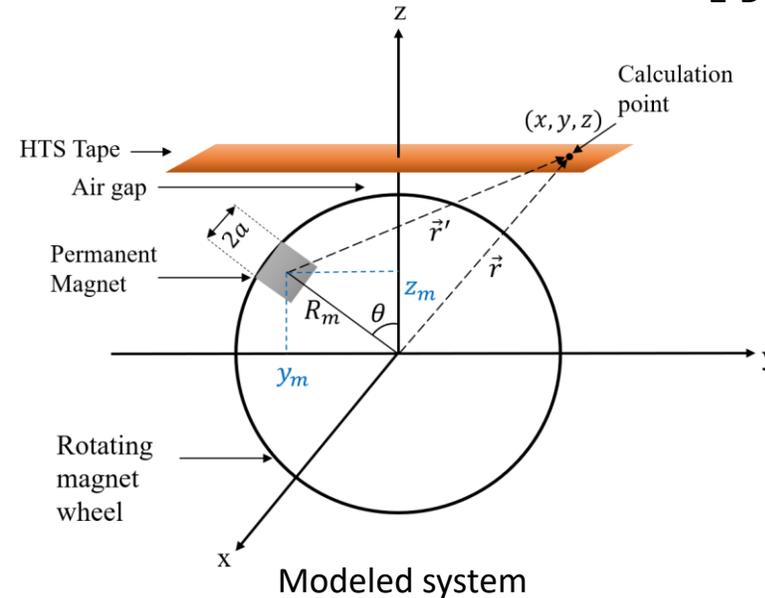


- Source magnetic-flux density:

$$\vec{B}_z^s = \frac{B^r}{4\pi} \sum_{i=0}^1 \sum_{j=0}^1 \sum_{k=0}^1 (-1)^{i+j+k} \text{atan2}(ST, RU) \vec{e}_z$$

$$\begin{cases} S = x - (-1)^i a \\ T = (y + R_m \sin\theta) - (-1)^j a \\ U = (z - R_m \cos\theta) - (-1)^k a \\ R = \sqrt{S^2 + T^2 + U^2} \end{cases}$$

$\theta = \Omega t$



System specifications

Parameter	Value	Description
$L / W / T$	50 4 0.1 mm	Tape dimensions
a / R_m	2.5 22.5 mm	Geometry of the magnetic wheel
B^r	1.4 T	Remanent magnetization of magnets
Ω	826.73 rad/s	Angular speed of the magnet wheel

Modeling

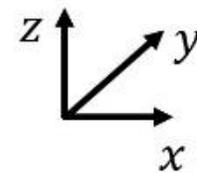
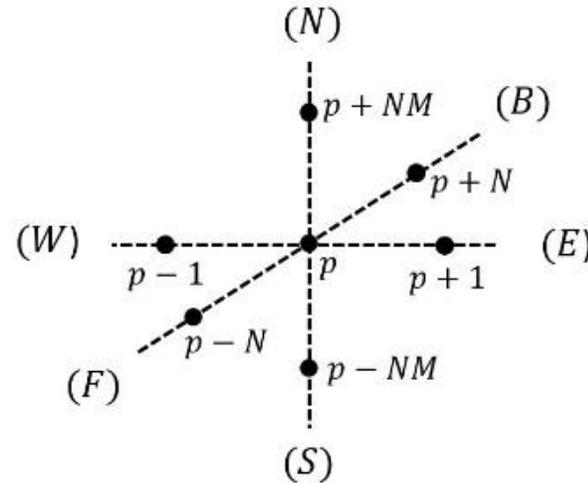
Thermal model

- Diffusion equation:

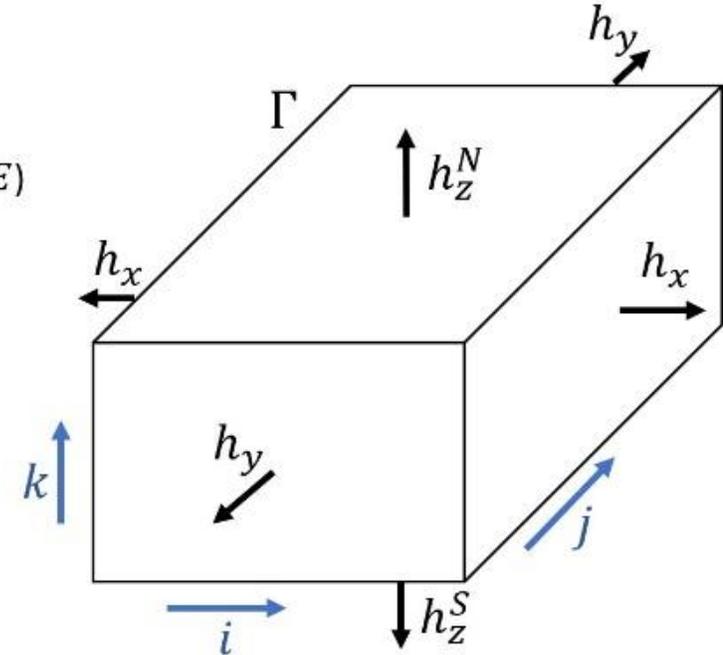
$$\begin{cases} \gamma C_p \frac{\partial T}{\partial t} = \frac{\partial}{\partial x} \left(\lambda \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left(\lambda \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z} \left(\lambda \frac{\partial T}{\partial z} \right) + \mathcal{P} \\ -\lambda \vec{\nabla} T \cdot \vec{n} = h(T - T_e), \quad \text{on } \Gamma \end{cases}$$

- Boundary conditions:

$$\begin{cases} \lambda_W \frac{\partial T}{\partial x} \Big|_W = h_x(T_p - T_e) \\ -\lambda_E \frac{\partial T}{\partial x} \Big|_E = h_x(T_p - T_e) \\ \lambda_F \frac{\partial T}{\partial y} \Big|_F = h_y(T_p - T_e) \\ -\lambda_B \frac{\partial T}{\partial y} \Big|_B = h_y(T_p - T_e) \\ \lambda_S \frac{\partial T}{\partial z} \Big|_S = h_z^S(T_p - T_e) \\ -\lambda_N \frac{\partial T}{\partial z} \Big|_N = h_z^N(T_p - T_e) \end{cases}$$



Finite difference discretization strategy

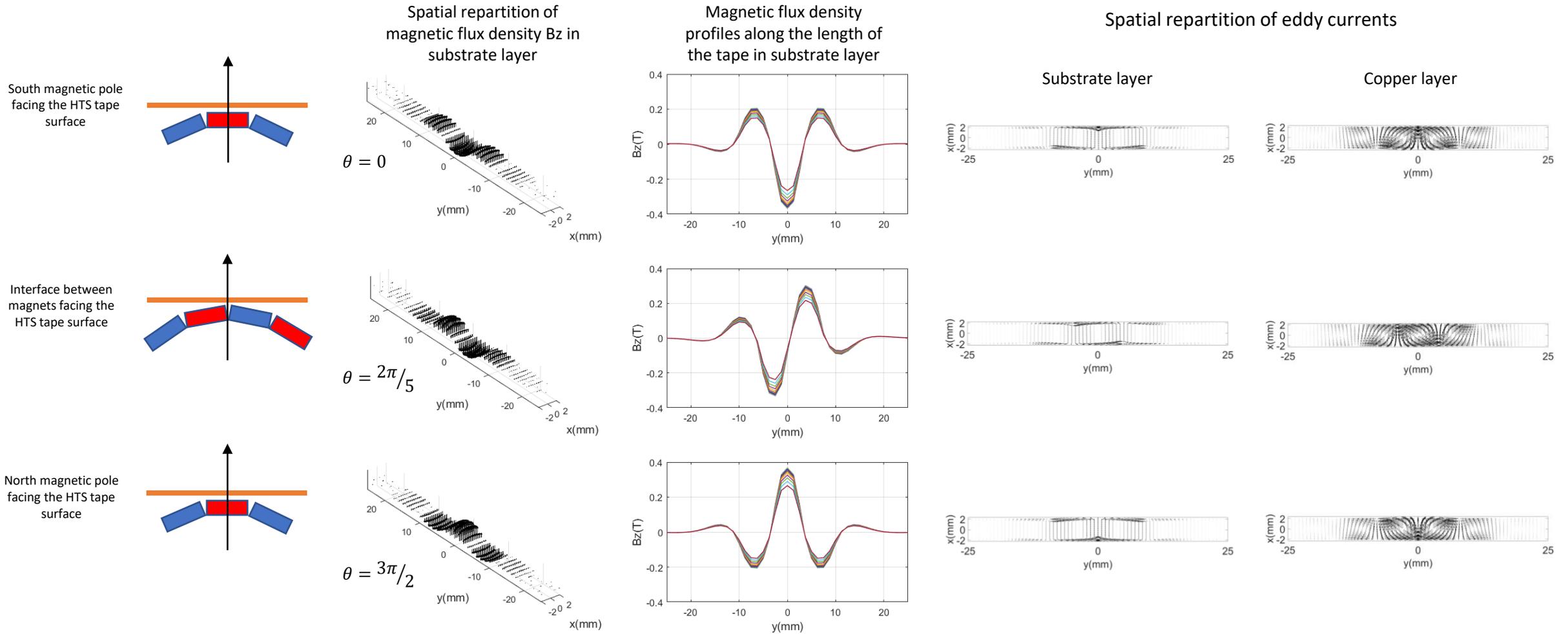


Global index:

$$p = i + (j - 1)N + (k - 1)NM$$

where $(1 \leq i \leq N, 1 \leq j \leq M, 1 \leq k \leq L)$

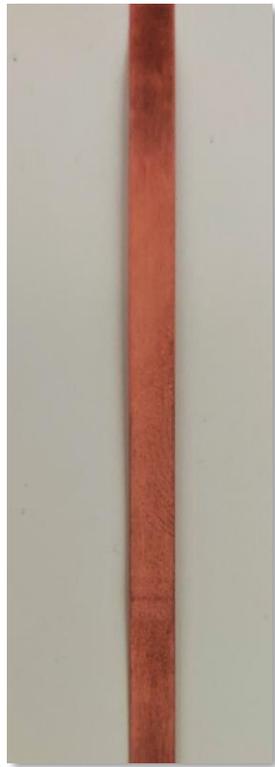
Results and validation



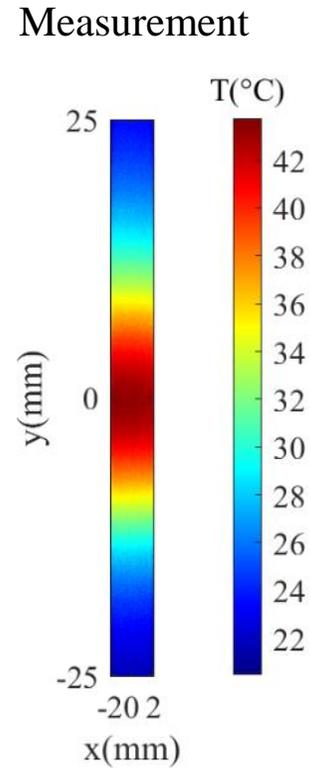
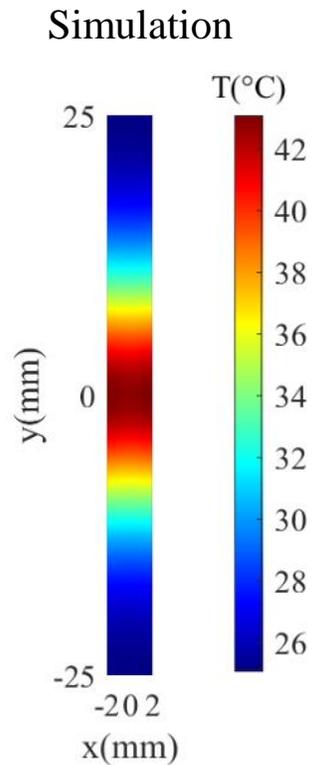
Evolution of the electromagnetic quantities as a function of the wheel position

Results and validation

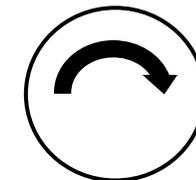
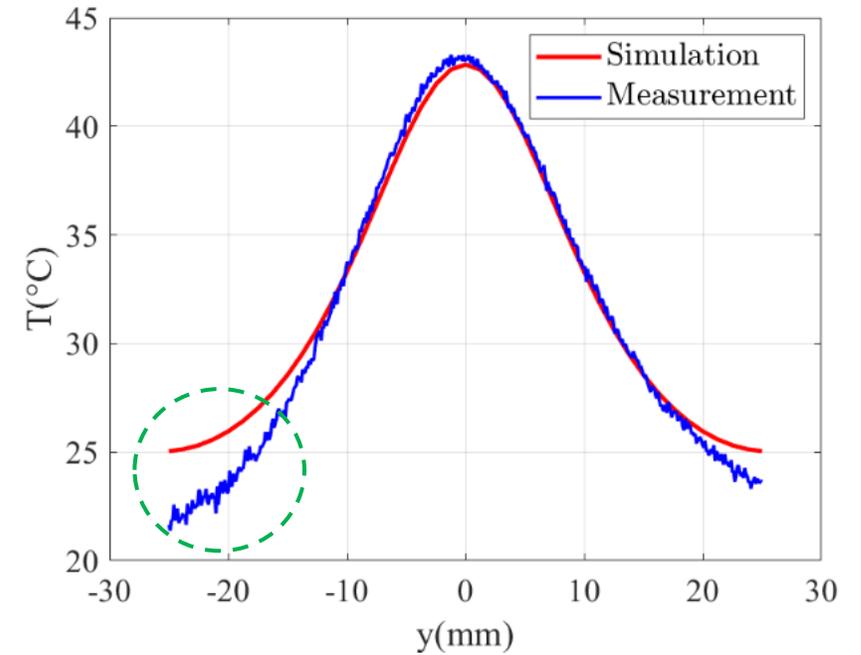
- Unflawed HTS tape:



Photograph of the HTS tape



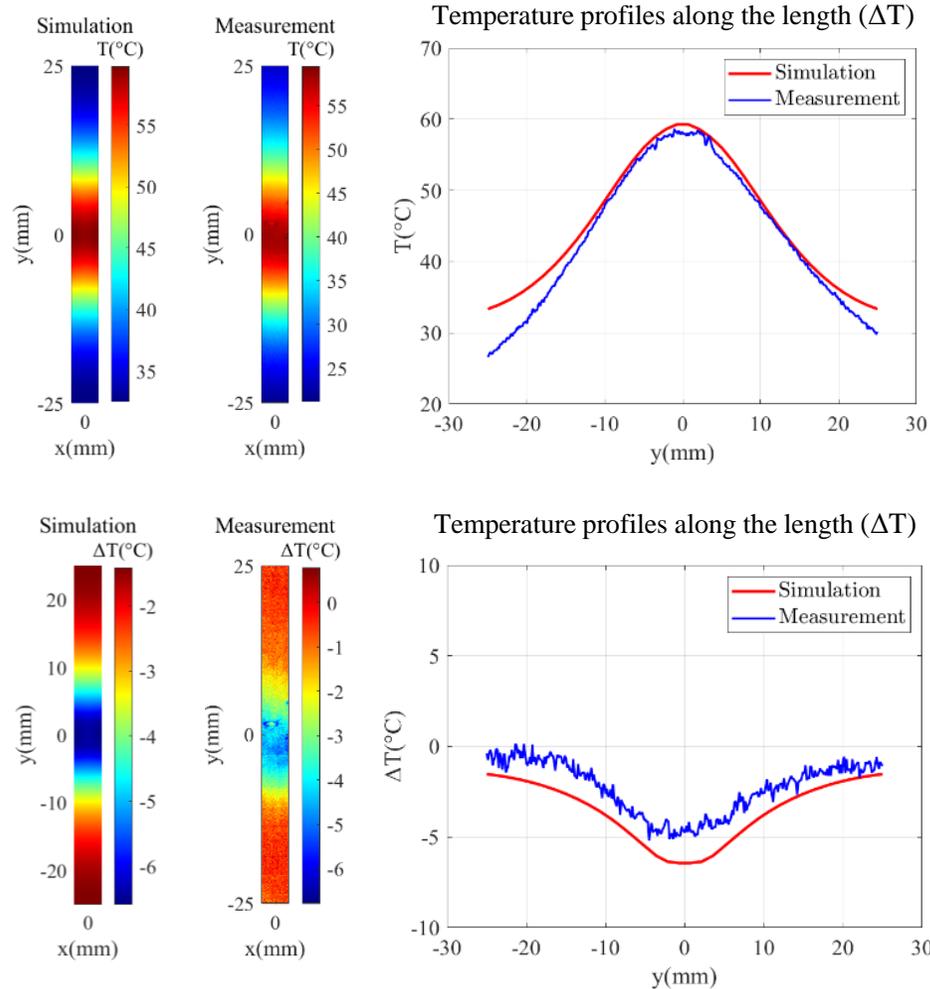
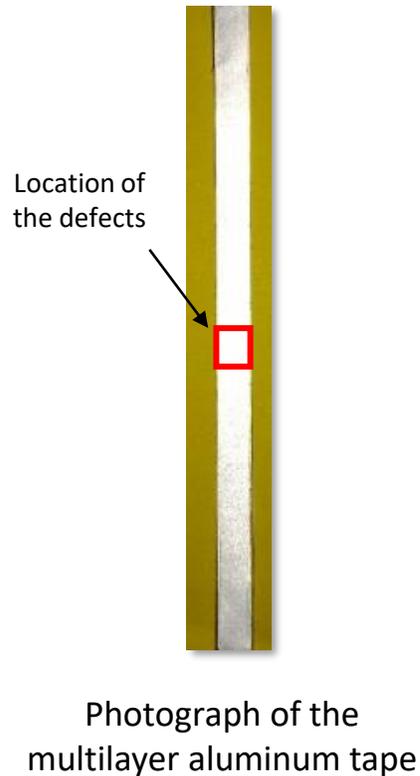
Temperature profiles along the length



The direction of the rotation of the magnetic wheel

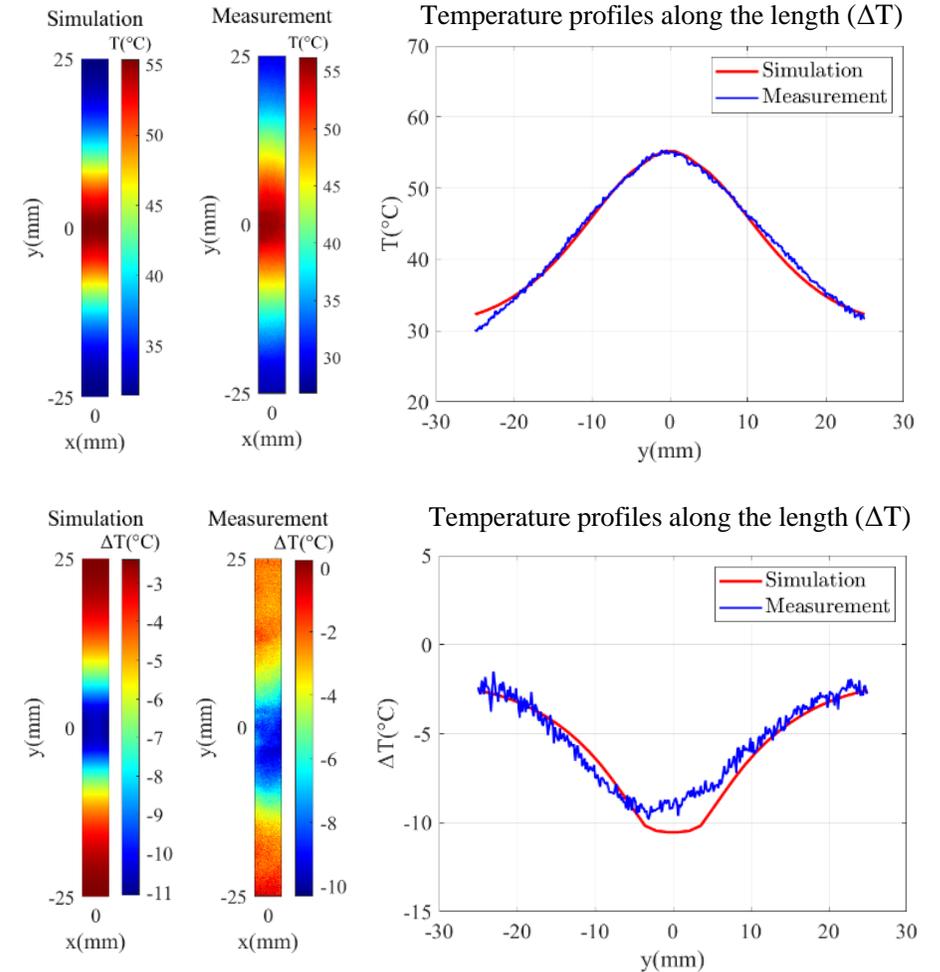
Results and validation

- Delamination defect: 5 mm x 5 mm x 20 μm



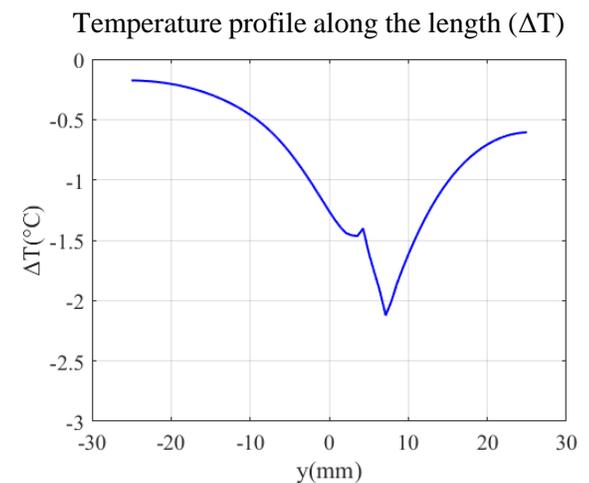
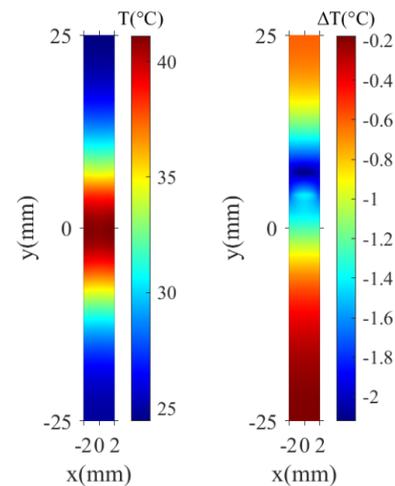
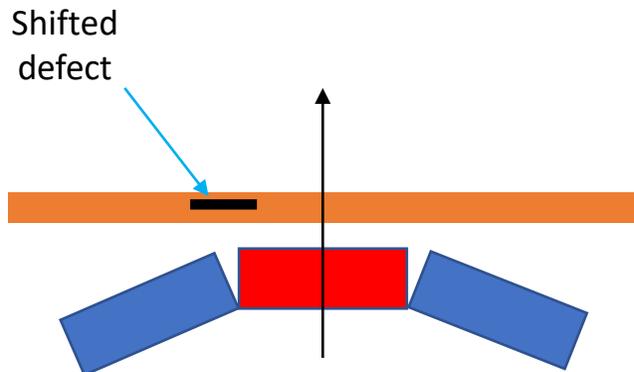
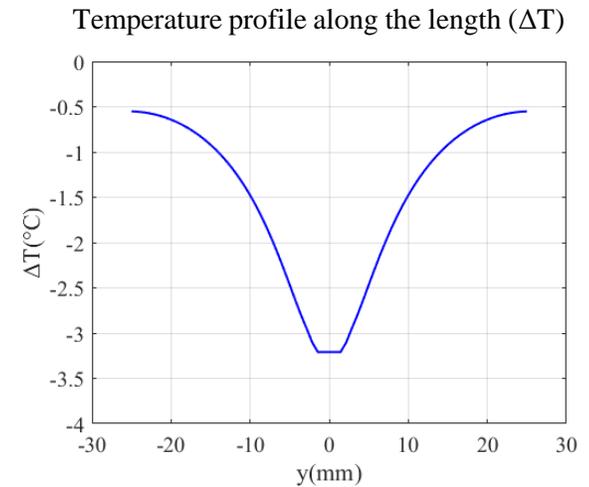
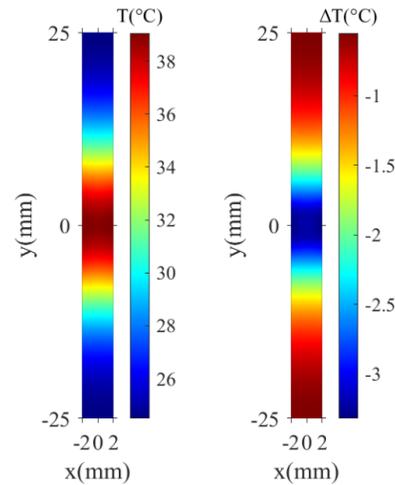
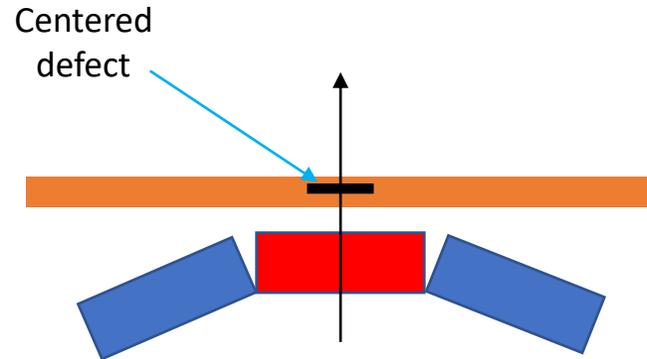
- Pore defect: 5 mm x 5 mm x 30 μm

$$\vec{n} \times \vec{T} = \vec{0}|_{\Gamma_d}$$



Results and validation

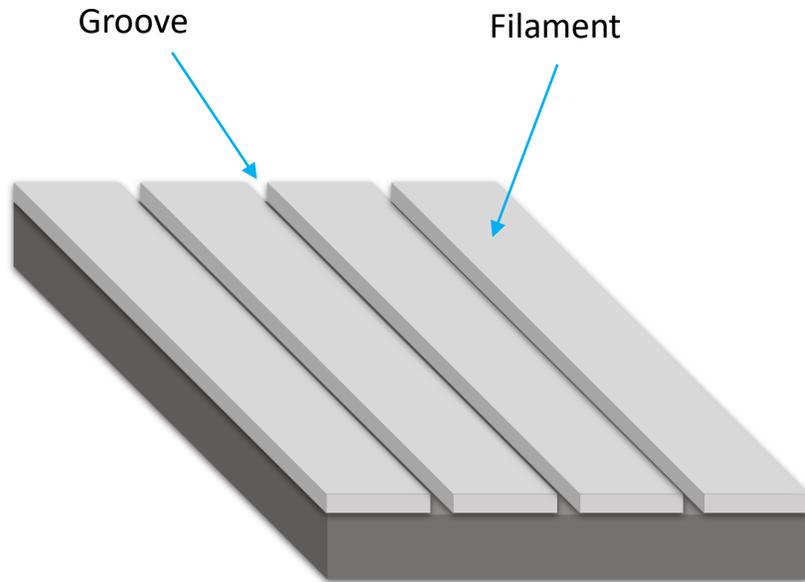
- Simulation of delamination defect in HTS tape: 3.4 mm x 3.6 mm x 30 μm



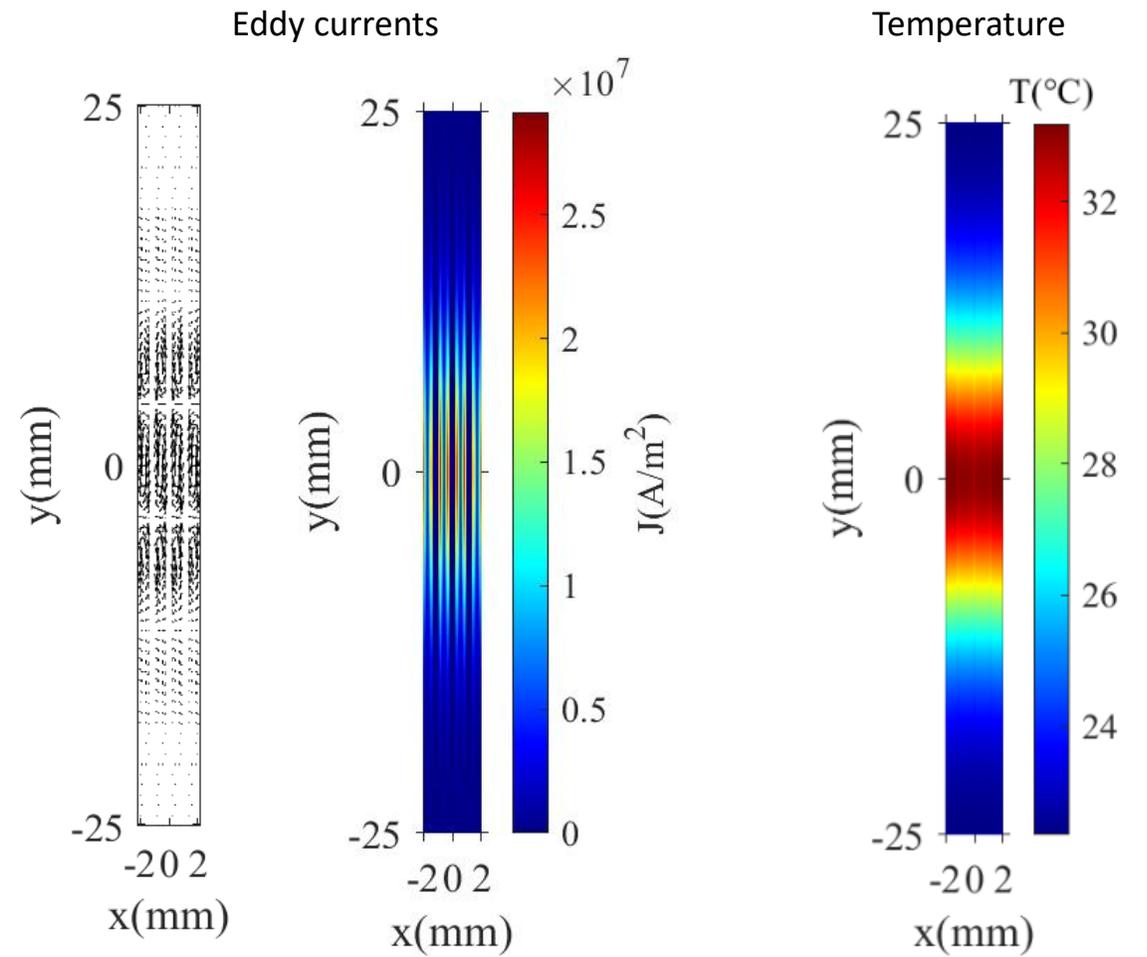
Results and validation

- Control of grooves in striated HTS tape:

Ideal grooves:

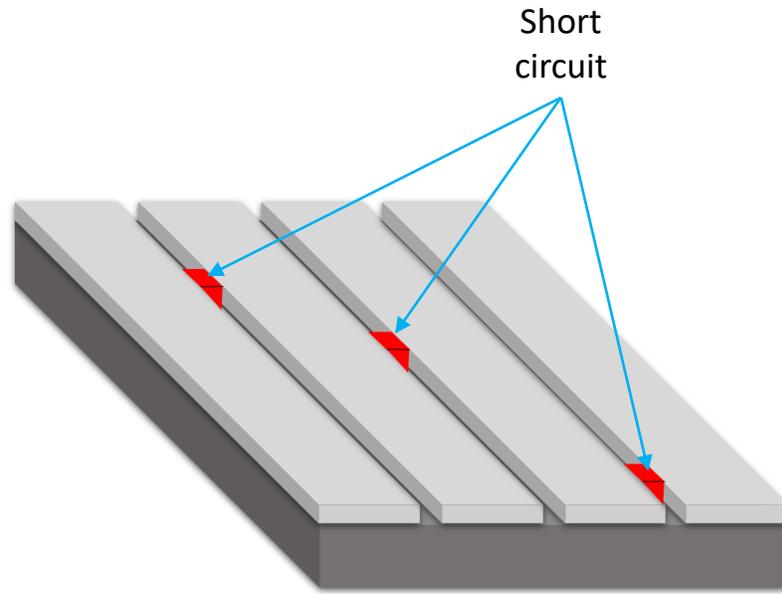


Unflawed striated HTS tape

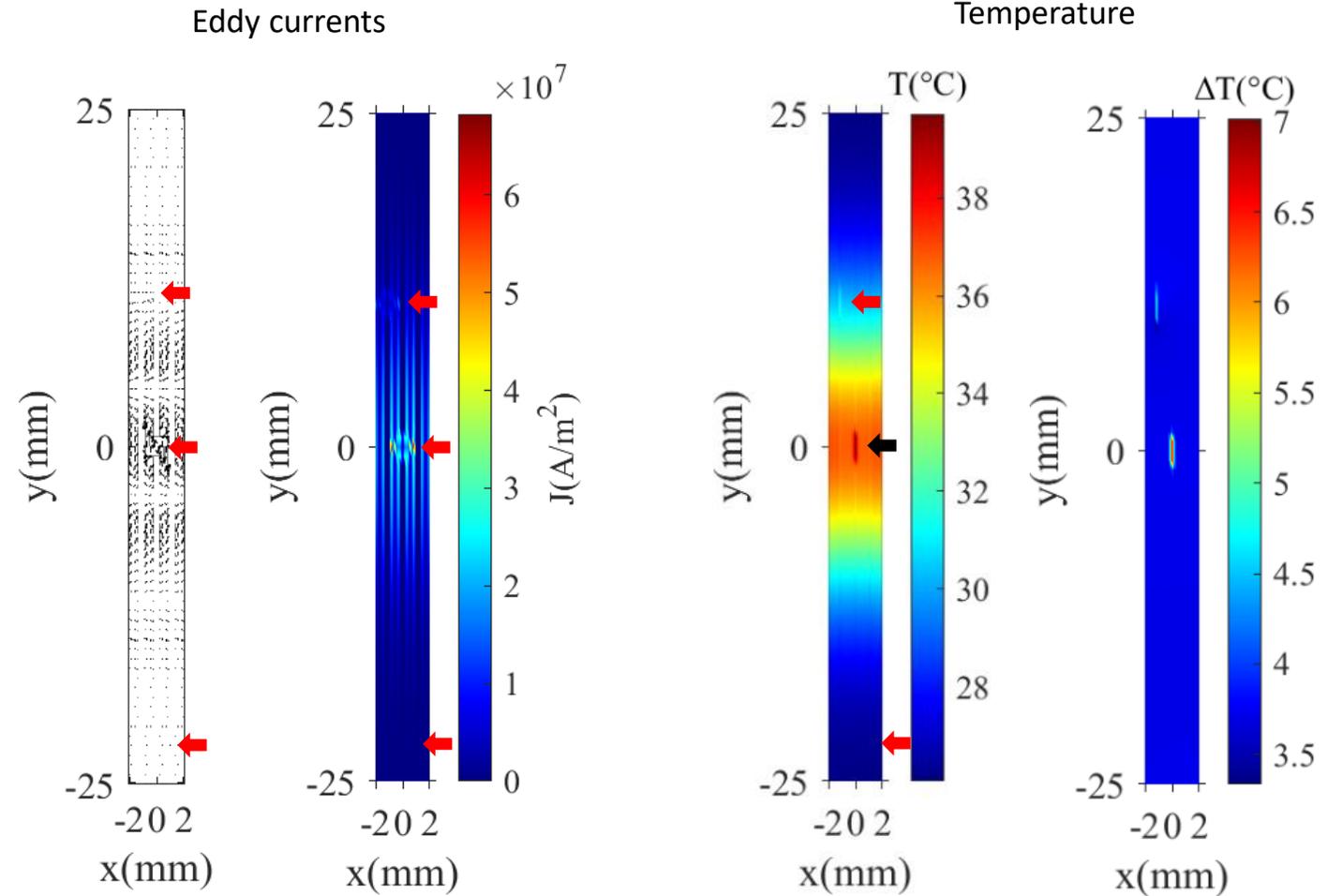


Results and validation

- Control of grooves in striated HTS tape:
Short circuit between filaments :

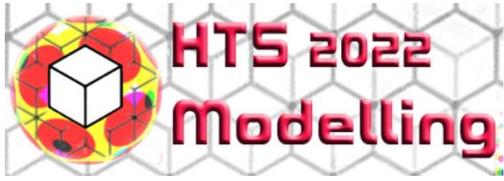


Striated HTS tape presenting short circuits between filaments



Conclusion

- Numerical and experimental investigations of structural control in 2G HTS tapes **at room temperature** using eddy current thermography.
- Highlighting the possibility of detection of several types of defects.
- Efficient and rapid numerical modeling.
- Future work: experimental testing of flaws in 2G HTS tapes.



Thank you for your attention

Walid Dirahoui,  e-mail: walid.dirahoui@univ-lorraine.fr
